

# A Higher-Order Theory of Presupposition

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# Separate Traditions

- Sentence (or **static**) meaning (Montague, 1973):
  - distinction between sense and reference (cf. Frege, 1892)
  - well-understood formal foundations
  - compositional derivation of sentence meanings from their subparts
  - unified treatment of NP meanings, quantification, coordination

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  - well-understood formal foundations
  - compositional derivation of sentence meanings from their subparts
  - unified treatment of NP meanings, quantification, coordination
- Discourse (or **dynamic**) meaning (Kamp's (1981) DRT, Heim's (1982) FCS):
  - ability to handle cross-sentential and 'donkey' anaphora
  - account of the novelty condition on indefinites
  - characterization of natural language meaning as utterance use in context
  - ability to model presuppositions

## Combining Efforts

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- no formal resources beyond standard higher-order logic (HOL: Church, 1940)
  - ability to characterize static (sentence) meaning as well as discourse anaphora
- Cons**
- no way to model presuppositions more general than extremely simplified cases of definite anaphora

# Compositionality Revisited

- Frege not only noted that sentence meaning is compositional, but also that presuppositions ‘project’ through e.g. negation:

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- Frege called the phenomenon of presupposition an “imperfection” of language.
- But given that they project, we could think of the task of stating an utterance’s presuppositions as one of the aspects of compositionally determining meaning (separate from truth conditions).

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# What This Talk is About

- In this talk, I discuss my ongoing work with Carl Pollard to develop a more general theory of presupposition.
- Main idea: take inspiration from Muskens and de Groote to build a theory equipped to handle presuppositions as well as static and dynamic meaning.
- First I lay out some preliminaries, then show how our theory accounts for some selected kinds of presupposition (definite anaphora, factivity, ‘donkey’ anaphora).

# Approach

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**Strategy** ① Enrich the discourse context to include **discourse referents (DRs)** preordered by relative **salience** and a **common ground (CG)** of mutually accepted content (following Stalnaker (1973), Lewis (1979), and Roberts (1996)).

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- Strategy**
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  - 2 Model presuppositions (following Stalnaker, 1973; Heim, 1983a) as the conditions a discourse context must meet for an utterance's felicitous interpretation.

# Point of Departure

- Start with Pollard's (2008) static hyperintensional semantics, which is built on classical higher-order logic (HOL: Church, 1940; Henkin, 1950).
  - A finer-grained alternative to Montague semantics that fixes some foundational problems with it.
  - Assumes, following Thomason (1980), that propositions (type  $p$ ) are basic and worlds defined in terms of them (instead of the other way around, as for Montague).



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  - Assumes, following Thomason (1980), that propositions (type  $p$ ) are basic and worlds defined in terms of them (instead of the other way around, as for Montague).
- Then add
  - following Lambek and Scott (1986), separation subtyping and a natural number type  $\omega$  as the type of DRs (following Heim) in addition to the other basic types  $p$ ,  $t$  (of truth values), and  $e$  (of entities), and
  - dependent coproduct types parameterized by  $\omega$

# Discourse Contexts

- For each  $n : \omega$ , an  $n$ -context  $c_n$  is a triple of type

$$c_n =_{\text{def}} a_n \times r_n \times p$$

where

- ①  $a_n$  is an  $n$ -**anchor** mapping the first  $n$  DRs to entities,
- ②  $r_n$  is an  $n$ -**resolution** (a preorder on the first  $n$  DRs that encodes their relative salience), and
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  - 3  $p$  is a proposition (the CG).
- The umbrella type  $c$  is the dependent coproduct of all the  $c_n$ .

# Manipulating Contexts

For an  $n$ -context  $c$ :

- The functions  $\mathbf{a} : c \rightarrow a$ ,  $\mathbf{r} : c \rightarrow r$ , and  $\mathbf{p} : c \rightarrow p$  abbreviate the projections from  $c$  to its three components.

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- DRs are added to  $c$ 's anchor and resolution by  $::_n$ , so that  $(c ::_n x)$  is just like  $c$  except that
  - its anchor ( $\mathbf{a} c$ ) maps  $n$  to the entity  $x$ , and
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- $+$  extends a CG. For any proposition  $p$ , the CG of  $c + p$  is  $(\mathbf{p} c)$  and  $p$  (where and is propositional conjunction).



## Context-Dependent Propositions

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  - $c$  satisfies the presuppositions of  $k$ , or equivalently
  - $k$  is **felicitous** in  $c$ .
- Dynamic (declarative) sentence meanings are functions from CDPs to CDPs. Their type is

$$u =_{\text{def}} k \rightarrow k$$

(mnemonic for **update** or **utterance**).

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$$(\mathbf{dyn}_0 \text{ rain}) = \lambda_{kc}.\text{rain} \text{ and } (k (c + \text{rain}))$$

$$(\mathbf{dyn}_1 \text{ donkey}) = \lambda_{nkc}.\text{donkey } [n] \text{ and } (k (c + (\text{donkey } [n])))$$

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- So dynamic properties reflect the intuition that an utterance's interpretation both depends on and modifies the discourse context.
- Dynamic properties are written using smallcaps versions of their static counterparts, e.g. RAIN = ( $\mathbf{dyn}_0$  rain), etc.
- The type  $d_1$  of unary dynamic properties is abbreviated to  $d$ .



# Staticization

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- The **staticizer** function  $\mathbf{stat} : c \rightarrow u \rightarrow p$  takes care of this using the **trivial** CDP  $\lambda_c \mathbf{true}$  to 'discard' the discourse context:

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- Example (here  $\equiv$  is propositional equivalence):

$$\begin{aligned} (\mathbf{stat} c \text{ RAIN}) &= (\lambda_{kc}(\text{rain and } (k (c + \text{rain})))) \lambda_c \mathbf{true} c \\ &= \text{rain and } (\lambda_c \mathbf{true} (c + \text{rain})) \\ &= \text{rain and true} \\ &\equiv \text{rain} \end{aligned}$$

## Dynamic Conjunction

Conjunction is designed to allow the first conjunct to satisfy the presuppositions of the second:

$$\text{AND} =_{\text{def}} \lambda_{uvk}.u (v k) : u \rightarrow u \rightarrow u$$

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- For example, the discourse *It rains. It pours.* is analyzed as the following update:

$$\begin{aligned} & \text{RAIN AND POUR} : u \\ & = \lambda_{kc}.(\lambda_{kc}(\text{rain and } k (c + \text{rain})) \lambda_c(\text{pour and } (k (c + \text{pour})))) c \\ & = \lambda_{kc}.\text{rain and pour and } k (c + \text{rain} + \text{pour}) \end{aligned}$$

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- Note that *rain* is available in the CG of the context passed to *POUR*

# Dynamic Existential Quantifier

The **dynamic existential** introduces DRs:

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- The dynamic indefinite article uses EXISTS to pass a newly introduced DR to its restrictor and scope (both dynamic properties):

$$A =_{\text{def}} \lambda_{DE}.\text{EXISTS } \lambda_n.(D n) \text{ AND } (E n) : d \rightarrow d \rightarrow u$$



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- Since EXISTS introduces an as-yet-unused DR, this definition of the dynamic indefinite captures Heim's novelty condition on indefinites.

# Dynamic Indefinite Example

Example for *A donkey brays*, where  $\text{BRAY} = (\mathbf{dyn}_1 \text{ bray})$ :

$$\begin{aligned}
 & \text{A DONKEY BRAY : u} \\
 & = \text{EXISTS } \lambda_n. (\text{DONKEY } n) \text{ AND } (\text{BRAY } n) \\
 & = \lambda_{kc}. \text{exists } \lambda_x. ((\text{DONKEY } (\text{next } c)) \text{ AND } (\text{BRAY } (\text{next } c))) k (c :: x) \\
 & = \lambda_{kc}. \text{exists } \lambda_x. (\text{donkey } x) \text{ and } (\text{bray } x) \\
 & \quad \text{and } (k (c :: x + (\text{donkey } x) + (\text{bray } x)))
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- Not only is the newly introduced DR (mapped to  $x$ ) available to the rest of the discourse, but so is the information that  $x$  is a braying donkey.

## Dynamic Negation

The **dynamic negation**  $\text{NOT} : u \rightarrow u$  ‘traps’ modifications made to the context under its scope using the staticizer:

$$\text{NOT} =_{\text{def}} \lambda_{uk} \lambda_c | (u k) \downarrow c. (\text{not} (\text{stat } c u)) \text{ and } (k (c + \text{not} (\text{stat } c u)))$$

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Example for the discourse *It is not raining*:

$$\begin{aligned} & \text{NOT RAIN} : u \\ &= \lambda_k \lambda_c | (\text{RAIN } k) \downarrow_c. (\text{not} (\text{stat } c \ \text{RAIN})) \text{ and } (k (c + (\text{not} (\text{stat } c \ \text{RAIN})))) \\ &= \lambda_k \lambda_c | (\text{RAIN } k) \downarrow_c. (\text{not rain}) \text{ and } (k (c + (\text{not rain}))) \end{aligned}$$

# Negation and Accessibility

The dynamic universal EVERY :  $d \rightarrow d \rightarrow u$  is built on NOT:

$$\text{EVERY} =_{\text{def}} \lambda_{DE}.\text{NOT} (\text{EXISTS } \lambda_n.(D n) \text{ AND } (\text{NOT} (E n)))$$

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where  $\varpi = \text{not} (\text{exists } \lambda_x.(\text{donkey } x) \text{ and } (\text{not} (\text{bray } x)))$  is the proposition added to the CG.



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- Note that no new DR is available to the subsequent discourse.
- So AND and NOT together represent this theory's counterpart of DRT accessibility.

## Sucky Weather

- (1) a. Pedro thinks it's raining.  
b. But it's not raining.
  - (2) a. It sucks that it's raining.  
b. # But it's not raining.
  - (3) a. It doesn't suck that it's raining.  
b. # But it's not raining.
- The difference in felicity between (1) and (2-3) has to do with the **factivity** of the verb *suck*: it presupposes the proposition expressed by its complement sentence.
  - Since (in 3) these presuppositions project through negation, we can't simply say *It sucks that it's raining* entails that it's raining.

# Modeling Factivity

The dynamic meaning of the factive *suck* is  $\text{SUCK} : u \rightarrow u$ :

$$\text{SUCK} =_{\text{def}} \lambda_{uk} \lambda_c | (\mathbf{p} \ c) \text{ entails } (\mathbf{stat} \ c \ u) \cdot (\mathbf{suck} \ (\mathbf{stat} \ c \ u)) \\ \text{and } (k \ (c + (\mathbf{suck} \ (\mathbf{stat} \ c \ u))))$$

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Note the condition on  $c$ : it requires that the CG entails the staticization of  $\text{SUCK}$ 's complement. Example for *It sucks that it rains*:

$$\text{SUCK RAIN} = \lambda_k \lambda_c | (\mathbf{p} \ c) \text{ entails } \text{rain} \cdot (\text{suck} \ \text{rain}) \text{ and } (k (c + (\text{suck} \ \text{rain}))) : u$$

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*Suck*'s factive presuppositions also project through negation:

$$\text{NOT } (\text{SUCK RAIN}) : u \\ = \lambda_k \lambda_c | (\text{SUCK RAIN } k) \downarrow_c \cdot (\text{not } (\text{suck } \text{rain})) \text{ and } (k (c + \text{not } (\text{suck } \text{rain})))$$

So the infelicity in both (2b) and (3b) is accounted for.

# Definiteness

- (4) # He thinks it's raining.
- (5) a. A farmer bought the donkey.  
 b. What donkey?  
 c. # Just some donkey I saw when we passed through Findlay.
- (6) a. A farmer bought a donkey and a mule.  
 b.  $\left\{ \begin{array}{l} \text{The donkey} \\ \# \text{ It} \end{array} \right\}$  brayed.

- Example (4), uttered out of the blue, shows the **familiarity** presupposition of definiteness (Heim, 1983b).
- But (5) and (6) show that familiarity isn't enough: the antecedent must be uniquely maximally **salient** (Roberts, 2005).

# Modeling the Definiteness of *It*

The dynamic definite pronoun meaning  $IT : d \rightarrow u$  is as follows (here  $NONHUMAN = (\mathbf{dyn}_1 \text{ nonhuman})$ ):

$$IT =_{\text{def}} \lambda_{Dkc}.D(\mathbf{def} \ c \ NONHUMAN) \ k \ c$$



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where  $\mathbf{def}_n : c_n \rightarrow d \rightarrow \omega_n$  picks out the most salient DR in a context  $c$  that is entailed by  $c$ 's CG to have the property  $D$ :

$$\mathbf{def}_n =_{\text{def}} \lambda_{cD}. \bigsqcup_{(\mathbf{r} \ c)} \lambda_{i:\omega_n}. (\mathbf{p} \ c) \text{ entails } (\mathbf{stat} \ c \ (D \ i))$$

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- This means that  $IT$  selects the uniquely most salient  $NONHUMAN$  DR in the discourse context, accounting for both the presupposition of familiarity and of unique greatest salience.

# Example of IT in Action

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*It brays* is analyzed as follows:

$$\begin{aligned}
 & \text{IT BRAY : u} \\
 & = \lambda_{kc}.\text{BRAY}(\mathbf{def} \ c \ \text{NONHUMAN}) \ k \ c \\
 & = \lambda_{kc}.\text{(bray} \ [(\mathbf{def} \ c \ \text{NONHUMAN})]) \ \text{and} \ (k \ (c \ + \ (\text{bray} \ [(\mathbf{def} \ c \ \text{NONHUMAN})])))
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=  $\lambda_{kc}.$ BRAY (**def**  $c$  NONHUMAN)  $k$   $c$

=  $\lambda_{kc}.$ (bray [(**def**  $c$  NONHUMAN)]) and ( $k$  ( $c$  + (bray [(**def**  $c$  NONHUMAN)])))

- Provided that the CG contains the information that donkeys are nonhuman, and no inferrably nonhuman DR more salient than (next  $c$ ), we can reduce (**def**  $c$  NONHUMAN) to  $x$ .

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 \end{aligned}$$

- Provided that the CG contains the information that donkeys are nonhuman, and no inferrably nonhuman DR more salient than (next  $c$ ), we can reduce ( $\mathbf{def} \ c \ \text{NONHUMAN}$ ) to  $x$ .
- Then the analysis of *A donkey enters. It brays.* is

$$\begin{aligned}
 & (\text{A DONKEY ENTER}) \ \text{AND} \ (\text{IT BRAY}) : u \\
 & = \lambda_{kc}.\text{exists } \lambda_x.\text{(donkey } x) \ \text{and} \ (\text{enter } x) \ \text{and} \ (\text{bray } x) \\
 & \quad \text{and} \ (k \ (c :: x + (\text{donkey } x) + (\text{enter } x) + (\text{bray } x)))
 \end{aligned}$$

# Modeling *The*

The dynamic meaning  $\text{THE} : d \rightarrow d \rightarrow u$  is similar to IT:

$$\vdash \text{THE} = \lambda_{DEkc} . (\lambda_n ((D n) \text{ AND } (E n)) (\mathbf{def} \ c \ D)) \ k \ c$$

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- $\text{THE}$  also resembles the dynamic indefinite  $\text{A}$ , except that it selects an antecedent based on  $D$  rather than introducing a new DR.
- Unlike  $\text{IT}$ , the two properties  $D$  and  $E$  are conjoined to make sure any DRs introduced by the first are available to the second (as in *The donkey with the red blanket chews it.*).

## The in Action

The analysis of *The donkey brays* is:

$$\begin{aligned}
 & (\text{THE DONKEY BRAY}) : \mathbf{u} \\
 & = \lambda_{kc}.(\lambda_n((\text{DONKEY } n) \text{ AND } (\text{BRAY } n)) (\mathbf{def } s \text{ DONKEY})) k c \\
 & = \lambda_{kc}.(\text{donkey } [(\mathbf{def } c \text{ DONKEY})]) \text{ and } (\text{bray } [(\mathbf{def } c \text{ DONKEY})]) \\
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- The upshot is that, in a discourse like *A donkey enters. A mule enters. The donkey brays.*, THE DONKEY is able to select the ‘right’ antecedent (the one that is a donkey).

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- The upshot is that, in a discourse like *A donkey enters. A mule enters. The donkey brays.*, THE DONKEY is able to select the ‘right’ antecedent (the one that is a donkey).
- The discourse *A donkey enters. A mule enters. #It brays.* is correctly predicted to be infelicitous, because IT has no way of deciding which of the two nonhuman DRs to select.

## Speaking of Donkeys ...

The notorious ‘donkey sentences’ pose problems for semantic interpretation:

- (7) a. Every farmer who owns a donkey beats it.  
b. # It’s named “Chiquita.”

- For (7a), we have to say how the DR introduced in the restriction can antecede the pronoun *it* in the scope.
- But we can’t just say that indefinites make a DR ‘globally’ available (7b)!

# Handling Donkey Anaphora I

- To analyze (7), we first need

FARMER = (**dyn**<sub>1</sub> farmer)

OWN = (**dyn**<sub>2</sub> own)

DONKEY = (**dyn**<sub>1</sub> donkey)

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- Next, we define the dynamic meaning of WHO :  $d \rightarrow d \rightarrow d$  as the conjunction of two (dynamic) properties:

WHO =<sub>def</sub>  $\lambda_{DEn}.(E n) \text{ AND } (D n)$

## Handling Donkey Anaphora II

We use the HOL rules Hypothesis and Abstraction (in addition to Application) to get the dynamic meaning of (7):

$$\begin{aligned}
 & (\text{EVERY (WHO } \lambda_j (\text{A DONKEY } \lambda_i (\text{OWN } i j)) \text{ FARMER)} \lambda_j . \text{IT } \lambda_i . \text{BEAT } i j) : u \\
 & = \lambda_{kc} . (\text{not (exists } \lambda_x ((\text{farmer } x) \text{ and (exists } \lambda_y ((\text{donkey } y) \text{ and (own } y x) \\
 & \quad \text{and (not (beat } y x)))))) \text{ and } k (c + \varpi)
 \end{aligned}$$

(note that this is the ‘strong donkey’ reading). Here the context passed to the subsequent discourse is extended with the proposition

$$\begin{aligned}
 \varpi = & \text{not (exists } \lambda_x . (\text{farmer } x) \text{ and (exists } \lambda_y . (\text{donkey } y) \text{ and (own } y x) \\
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 \end{aligned}$$

- So IT is able to select its nonhuman antecedent, but no DR remains in the resulting discourse context.

## Taking Stock

- This new theory combines Montague's static compositionality with DRT innovations like the ability to characterize cross-sentential and 'donkey' anaphora, using no formal resources beyond classical HOL.
- But unlike earlier attempts to do this, it also has a more general way to capture an utterance's presuppositions by stating them as conditions on the discourse context.
- The payoff is a better handling of definite anaphora and a way to characterize other presuppositional phenomena like projection and factivity.

## What's Next

- Make the theory *truly* compositional by hooking it up with a grammar.
- Figure out how to model the “proportion problem” (a.k.a. “farmer-donkey asymmetry”) associated with e.g. *most* in this setup. This will likely involve going beyond the ‘strong donkey’ reading we currently get.
- Find a way to say how the relative salience of DRs gets adjusted as the discourse unfolds.
- Give a computational implementation of a fragment of English using this theory.
- Model more kinds of presuppositions: e.g., those associated with proper names, *too*, etc.

# Thanks

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# Bibliography

## I

- Alonzo Church. A formulation of the simple theory of types. *Journal of Symbolic Logic*, 5:56–68, 1940.
- Philippe de Groote. Towards a Montagovian account of dynamics. In *Proceedings of Semantics and Linguistic Theory 16*, 2006.
- Philippe de Groote. Typing binding and anaphora: Dynamic contexts as  $\lambda\mu$ -terms. Presented at the ESSLLI Workshop on Symmetric Calculi and Ludics for Semantic Interpretation, 2008.
- Gottlob Frege. Über Sinn und Bedeutung. *Zeitschrift für Philosophie und philosophische Kritik*, pages 25–50, 1892. English translation in P. Geach and M. Black, editors, *Translations from the Philosophical Writings of Gottlob Frege*, Blackwell, Oxford, 1952.
- Irene Heim. *The Semantics of Definite and Indefinite Noun Phrases*. PhD thesis, University of Massachusetts, Amherst, 1982.

# Bibliography

## II

- Irene Heim. On the projection problem for presuppositions. In M. Barlow, D. Flickinger, and M. Westcoat, editors, *WCCFL2: Second Annual West Coast Conference on Formal Linguistics*. Stanford University, Stanford, California, 1983a.
- Irene Heim. File change semantics and the familiarity theory of definiteness. In *Meaning, Use and the Interpretation of Language*. Walter de Gruyter, Berlin, 1983b.
- Leon Henkin. Completeness in the theory of types. *Journal of Symbolic Logic*, 15:81–91, 1950.
- Hans Kamp. A theory of truth and semantic representation. In J. Groenendijk, T. Janssen, and M. Stokhof, editors, *Formal Methods in the Study of Language*. Mathematisch Centrum, Amsterdam, 1981.

# Bibliography

## III

Joachim Lambek and Phil Scott. *Introduction to Higher-Order Categorical Logic*. Cambridge University Press, 1986.

David Lewis. Scorekeeping in a language game. In R. Bäuerle, U. Egli, and A. von Stechow, editors, *Semantics from a Different Point of View*. Springer, Berlin, 1979.

Richard Montague. The proper treatment of quantification in ordinary English. In K. Hintikka, J. Moravcsik, and P. Suppes, editors, *Approaches to Natural Language*. D. Reidel, Dordrecht, 1973.

Reinhard Muskens. Categorical Grammar and Discourse Representation Theory. In *Proceedings of COLING*, 1994.

Reinhard Muskens. Combining Montague semantics and discourse representation theory. *Linguistics and Philosophy*, 19:143–186, 1996.

# Bibliography

## IV

- Carl Pollard. Hyperintensions. *Journal of Logic and Computation*, 18 (2):257–282, 2008.
- Craige Roberts. Information structure in discourse: Towards an integrated formal theory of pragmatics. In *Papers in Semantics*, number 49 in Working Papers in Linguistics. Ohio State University Department of Linguistics, 1996.
- Craige Roberts. Pronouns as definites. In M. Reimer and A. Bezuidenhout, editors, *Descriptions and Beyond*. Oxford University Press, 2005.
- Robert Stalnaker. Presuppositions. *Journal of Philosophical Logic*, 2 (4), 1973.
- Richmond Thomason. A model theory for propositional attitudes. *Linguistics and Philosophy*, 4:47–70, 1980.